# Productive Density and Distribution from an Input-Output Perspective: The Case of Argentina since the 1950s 

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## Context and motivation

Context and motivation:
$\triangleright$ Long-run history of the conflictive relationship between trade balance (and BoP) constraints and productive structure ('densidad productiva') in Latin America
$\triangleright$ 'Competitiveness': issue related to relative price and distribution structure of the economy (at least, partially)
$\triangleright$ Argentina since the 1950s: succession of 6 economic regimes
(i) Import-substitution industrialisation (early 10950s)
(ii) Structuralism ('desarrollismo', late 1950s to mid 1970s)
(iii) Economic Liberalisation (late 1970s - early 1980s)
(iv) Debt-crisis inflationary economy (1980s)
(v) Convertibility (1990s)
(vi) Post-Convertibility (2000s)

## Main contribution

$\triangleright$ Brody (1970) type of extended Input-Output scheme based on the computation of 'standard prices' (Pasinetti, 1992) - rather than 'standard proportions' (Sraffa, 1960)
$\triangleright$ Compute and analyse the structure of relative prices and distribution implied by a situation of balanced trade (for given quantities), to shed light on the constraints that productive structure pose on distributive possibilities
$\triangleright$ Apply the framework to the case of Argentina from 1950s onwards

## Structural expenditure and income accounting (I)

$$
\begin{aligned}
\mathbf{x} & =\mathbf{X e}+\mathbf{f} \\
\mathbf{x}^{T} & =\mathbf{e}^{T} \mathbf{X}+\mathbf{m}^{T}+\mathbf{w}^{T}+\boldsymbol{\pi}^{T} \\
\mathbf{X} & =\mathbf{A} \widehat{\mathbf{x}}=\left[a_{i j} x_{j}\right] \\
\mathbf{w}^{T} & =\mathbf{a}_{w}^{T} \widehat{\mathbf{x}}=\left[a_{w j} x_{j}\right] \\
\mathbf{m}^{T} & =\mathbf{a}_{m}^{T} \widehat{\mathbf{x}}=\left[a_{m j} x_{j}\right] \\
\boldsymbol{\pi}^{T} & =\mathbf{a}_{\pi}^{T}=\left[a_{\pi j} x_{j}\right] \\
\mathbf{f} & =\mathbf{f}_{c w}+\mathbf{f}_{e}+\mathbf{f}_{z} \\
\mathbf{f}_{c w} & =\boldsymbol{\theta}_{c} W, \quad \mathbf{f}_{e}=\boldsymbol{\theta}_{e} M \\
C & =\mathbf{e}^{T} \mathbf{f}_{c}+M_{c} \\
\boldsymbol{\theta}_{c} & =\mathbf{f}_{c} / C, \quad \theta_{c}^{m}=M_{c} / C \\
W & =\mathbf{a}_{w}^{T} \mathbf{X} \\
M & =\mathbf{a}_{m}^{T} \mathbf{x}+\theta_{c}^{m} W+M_{z}
\end{aligned}
$$

(Expenditure)
(Income)
(Intermediate inputs) (Industry wages)
(Intermediate imports)
(Surplus)
(Final demand)
(Wage-consumption \& Exports)
(Agg. final consumption)
(Consumption structure)
(Wage bill)
(Imports)

## Structural expenditure and income accounting (II)

Expenditure:

$$
\left[\begin{array}{c}
\mathbf{x} \\
W \\
M
\end{array}\right]=\left[\begin{array}{ccc}
\mathbf{A} & \boldsymbol{\theta}_{c} & \boldsymbol{\theta}_{e} \\
\mathbf{a}_{w}^{T} & 0 & 0 \\
\mathbf{a}_{m}^{T} & \theta_{c}^{m} & 0
\end{array}\right]\left[\begin{array}{c}
\mathbf{x} \\
W \\
M
\end{array}\right]+\left[\begin{array}{c}
\mathbf{f}_{z} \\
0 \\
M_{z}
\end{array}\right]
$$

Income:
$\left[\begin{array}{lll}\mathbf{e}^{T} & 1 & 1\end{array}\right]=\left[\begin{array}{lll}\mathbf{e}^{T} & 1 & 1\end{array}\right]\left[\begin{array}{ccc}\mathbf{A} & \boldsymbol{\theta}_{c} & \boldsymbol{\theta}_{e} \\ \mathbf{a}_{w}^{T} & 0 & 0 \\ \mathbf{a}_{m}^{T} & \theta_{c}^{m} & 0\end{array}\right]+\left[\begin{array}{lll}\mathbf{a}_{\pi}^{T} & 0 & \left(1-\mathbf{e}^{T} \boldsymbol{\theta}_{e}\right)\end{array}\right]$

## From structural price accounting to computable prices

Structural accounting:
$\left[\begin{array}{lll}\mathbf{e}^{T} & 1 & 1\end{array}\right]=\left[\begin{array}{lll}\mathbf{e}^{T} & 1 & 1\end{array}\right]\left[\begin{array}{ccc}\mathbf{A} & \boldsymbol{\theta}_{c} & \boldsymbol{\theta}_{e} \\ \mathbf{a}_{w}^{T} & 0 & 0 \\ \mathbf{a}_{m}^{T} & \theta_{c}^{m} & 0\end{array}\right]+\left[\begin{array}{lll}\mathbf{a}_{\pi}^{T} & 0 & \left(1-\mathbf{e}^{T} \boldsymbol{\theta}_{e}\right)\end{array}\right]$
Computable prices:

$$
\begin{aligned}
& {\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]=\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]\left[\begin{array}{ccc}
\mathbf{A} & \boldsymbol{\theta}_{c} & \boldsymbol{\theta}_{e} \\
\mathbf{a}_{w}^{T} & 0 & 0 \\
\mathbf{a}_{m}^{T} & \theta_{c}^{m} & 0
\end{array}\right]+} \\
& +r\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]\left[\begin{array}{lll}
\mathbf{A} & \mathbf{0} & \mathbf{0} \\
\mathbf{a}_{w}^{T} & 0 & 0 \\
\mathbf{a}_{m}^{T} & 0 & 0
\end{array}\right]
\end{aligned}
$$

## Computable prices: Interpretation

Developing the partitioned-matrix formulation:

$$
\begin{aligned}
& \mathbf{p}^{T}=(1+r)\left(\mathbf{p}^{T} \mathbf{A}+p_{w} \mathbf{a}_{w}^{T}+p_{m} \mathbf{a}_{m}^{T}\right) \quad \text { (Comm. prices) } \\
& p_{w}=\mathbf{p}^{T} \boldsymbol{\theta}_{c}+p_{m} \theta_{c}^{m} \quad(\text { Wage-labour monetary unit price) }
\end{aligned}
$$

$$
p_{m}=\mathbf{p}^{T} \boldsymbol{\theta}_{e} \quad \text { (Balanced foreign trade import price) }
$$

## Computable prices: solution

An eigensystem: $\mathbf{v}^{T} \neq \mathbf{0}^{T}$ such that:

$$
\lambda \mathbf{v}^{T}=\mathbf{v}^{T} \mathbf{M}
$$

Our system is:

$$
\begin{aligned}
& \frac{1}{r}\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]= \\
& =\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]\left(\left[\begin{array}{ccc}
\mathbf{A} & \mathbf{0} & \mathbf{0} \\
\mathbf{a}_{w}^{T} & 0 & 0 \\
\mathbf{a}_{m}^{T} & 0 & 0
\end{array}\right]\left[\begin{array}{ccc}
\mathbf{I}-\mathbf{A} & -\boldsymbol{\theta}_{c} & -\boldsymbol{\theta}_{e} \\
-\mathbf{a}_{w}^{T} & 1 & 0 \\
-\mathbf{a}_{m}^{T} & -\theta_{c}^{m} & 1
\end{array}\right]^{-1}\right)
\end{aligned}
$$

We can compute its solution:

$$
\left(r,\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]\right)
$$

## Computable prices: normalisation

Sum of all statistical unit-prices:

$$
\left[\begin{array}{lll}
\mathbf{e}^{T} & 1 & 1
\end{array}\right]\left[\begin{array}{l}
\mathbf{e} \\
1 \\
1
\end{array}\right]=\mathbf{e}^{T} \mathbf{e}+1+1=n+2
$$

Then, we want:

$$
\left[\begin{array}{lll}
\mathbf{p}^{T} & p_{w} & p_{m}
\end{array}\right]\left[\begin{array}{l}
\mathbf{e} \\
1 \\
1
\end{array}\right]=\mathbf{p}^{T} \mathbf{e}+p_{w}+p_{m}=n+2
$$

Thereby adopting:

$$
\frac{\mathbf{p}^{T} \mathbf{e}+p_{w}+p_{m}}{n+2}=1
$$

as the normalisation condition for the eigenproblem

## Examples in a $2 \times 2$ economy

|  | 1 | 2 | $C$ | $E$ | Oth. | $x$ |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10 | 5 | 1 | 2 | 1 | 19 |
| 2 | 5 | 15 | 2 | 4 | 0 | 26 |
| $m$ | 1 | 3 | 1 | 0 | 0 |  |
| $w$ | 2 | 1 |  |  |  |  |
| $\pi$ | 1 | 2 |  | 45 |  |  |
| $x$ | 19 | 26 |  |  |  |  |
| $B o T=E-M=6-5=1>0$ |  |  |  |  |  |  |
| $r=3 /(35+3+4)=0.071$ | (mark-up) |  |  |  |  |  |
| obs. |  |  |  |  | comp. | surplus |
| $p_{1}$ | 1.000 | 0.954 | 0.052 |  |  |  |
| $p_{2}$ | 1.000 | 0.931 | 0.076 |  |  |  |
| $p_{w}$ | 1.000 | 0.986 | 0.000 |  |  |  |
| $p_{m}$ | 1.000 | 1.127 | -0.200 |  |  |  |
| $r$ | 0.071 | 0.048 |  |  |  |  |

$B o T$ surplus: $\uparrow p_{m}, \downarrow p_{w}, \downarrow r$

|  | 1 | 2 | $C$ | $E$ | Oth. | $x$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10 | 5 | 1 | 2 | 1 | 19 |
| 2 | 5 | 15 | 2 | 4 | 0 | 26 |
| $m$ | 1 | 3 | 1 | 0 | 2 |  |
| $w$ | 2 | 1 |  |  |  |  |
| $\pi$ | 1 | 2 |  |  |  | 45 |
| $x$ | 19 | 26 |  |  |  |  |
| $=E-M=6-7=-1<0$ |  |  |  |  |  |  |

$r=3 /(35+3+4)=0.071$ (mark-up)

|  | obs. | comp. | surplus |
| :--- | ---: | ---: | ---: |
| $p_{1}$ | 1.000 | 1.078 | 0.052 |
| $p_{2}$ | 1.000 | 1.023 | 0.076 |
| $p_{w}$ | 1.000 | 1.004 | 0.000 |
| $p_{m}$ | 1.000 | 0.893 | 0.142 |
| $r$ | 0.071 | 0.089 |  |

$B o T$ deficit: $\downarrow p_{m}, \uparrow p_{w}, \uparrow r$

## Dataset characteristics: Argentina (1953-2011)

Table: Input-Output matrices for Argentina since the 1950s

| (all matrices in current AR\$, distinguishing between domestically produced and imported commodities) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Period | Year | Dimension | Source | Prices | GVA disag. |
| $1950-1958$ | 1953 | $23 \times 23$ | BCRA | Purchaser | Wages \& Salaries |
| $1959-1965$ | 1963 | $23 \times 23$ | BCRA | Purchaser | Wages \& Salaries |
| $1966-1974$ | 1973 | $56 \times 56$ | BCRA | Purchaser | Comp. Employees |
| $1983-1991$ | 1984 | $220 \times 220$ | BID-SP | Producer | - |
| $1991-2001$ | 1997 | $124 \times 124$ | INDEC | Basic | Comp. Employees |
| $2002-2007$ | 2004 | $95 \times 95$ | Own est. | Basic | Comp. Employees |
| $2008-2011$ | 2011 | $95 \times 95$ | Own est. | Basic | Comp. Employees |

## Argentina's Input-Output matrix: 1953

Cuadro 5

(Mgien de peses argentinoe)


## Industry Classification

| Industry Classification: 1953, 1973, 1997, 2011 |  |  |
| :---: | :---: | :---: |
| cod_IP | Description | Label |
| IP_01 | Agriculture | 01_AGRIC |
| IP_02 | Animal production | 02_ANIM |
| IP_03 | Mining | 03_MIN |
| IP_04 | Food processing | 04_FOOD |
| IP_05 | Tobacco | 05_TOBAC |
| IP_06 | Textiles \& apparel | 06_TEXT |
| IP_07 | Leather \& products | 07_LEATH |
| IP_08 | Wood \& Forestry Products | 08_WOOD |
| IP_09 | Paper products \& publishing | 09_PAPER |
| IP_10 | Chemicals | 10_CHEM |
| IP_11 | Petrochemical | 11_PETRO |
| IP_12 | Rubber \& Plastics | 12_RUBPL |
| IP_13 | Mineral products | 13_MINPR |
| IP_14 | Metal products | 14_METAL |
| IP_15 | Vehicles \& Mech. Mach. | 15_MMACH |
| IP_16 | Electrical Machinery | 16_EMACH |
| IP_17 | Other manufacturing | 17_OMANU |
| IP_18 | Utilities | 18_UTIL |
| IP_19 | Construction | 19_CONST |
| IP_20 | Transport, Comm. \& Trade | 20_TRCOTR |
| IP_21 | Prof. \& Social Services | 21_SERV |

## Computable prices for Argentina (1953-2011)

|  | IP53 |  |  | IP73 |  |  | IP97 |  |  | IP11 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Industry | obs. | comp. | surplus | obs. | comp. | surplus | obs. | comp. | surplus | obs. | comp. | surplus |
| 01_AGRIC | 1.000 | 0.703 | 0.520 | 1.000 | 0.653 | 0.447 | 1.000 | 0.674 | 0.486 | 1.000 | 0.737 | 0.439 |
| 02_ANIM | 1.000 | 0.629 | 0.540 | 1.000 | 0.668 | 0.504 | 1.000 | 0.889 | 0.347 | 1.000 | 0.628 | 0.493 |
| 03_MIN | 1.000 | 0.952 | 0.345 | 1.000 | 0.769 | 0.447 | 1.000 | 0.519 | 0.583 | 1.000 | 0.569 | 0.556 |
| 04_FOOD | 1.000 | 1.040 | 0.179 | 1.000 | 1.013 | 0.122 | 1.000 | 1.180 | 0.162 | 1.000 | 1.035 | 0.175 |
| 05_TOBAC | 1.000 | 0.569 | 0.587 | 1.000 | 0.488 | 0.572 | 1.000 | 1.133 | 0.174 | 1.000 | 1.033 | 0.230 |
| 06_TEXT | 1.000 | 1.225 | 0.220 | 1.000 | 1.683 | 0.098 | 1.000 | 1.276 | 0.229 | 1.000 | 1.062 | 0.319 |
| 07_LEATH | 1.000 | 1.218 | 0.237 | 1.000 | 1.071 | 0.206 | 1.000 | 1.386 | 0.242 | 1.000 | 1.280 | 0.151 |
| 08_WOOD | 1.000 | 1.196 | 0.247 | 1.000 | 1.140 | 0.180 | 1.000 | 0.958 | 0.283 | 1.000 | 0.690 | 0.485 |
| 09_PAPER | 1.000 | 1.174 | 0.249 | 1.000 | 1.217 | 0.150 | 1.000 | 1.098 | 0.240 | 1.000 | 1.159 | 0.226 |
| 10_CHEM | 1.000 | 1.063 | 0.291 | 1.000 | 1.001 | 0.260 | 1.000 | 1.052 | 0.225 | 1.000 | 1.119 | 0.229 |
| 11_PETRO | 1.000 | 0.554 | 0.627 | 1.000 | 0.772 | 0.375 | 1.000 | 0.808 | 0.132 | 1.000 | 0.869 | 0.207 |
| 12_RUBPL | 1.000 | 1.154 | 0.266 | 1.000 | 0.924 | 0.302 | 1.000 | 1.090 | 0.261 | 1.000 | 1.218 | 0.210 |
| 13_MINPR | 1.000 | 1.064 | 0.271 | 1.000 | 0.998 | 0.239 | 1.000 | 0.961 | 0.273 | 1.000 | 0.874 | 0.308 |
| 14_METAL | 1.000 | 1.261 | 0.204 | 1.000 | 1.045 | 0.208 | 1.000 | 1.123 | 0.223 | 1.000 | 1.044 | 0.281 |
| 15_MMACH | 1.000 | 1.213 | 0.222 | 1.000 | 1.171 | 0.188 | 1.000 | 1.160 | 0.202 | 1.000 | 1.317 | 0.120 |
| 16_EMACH | 1.000 | 1.150 | 0.272 | 1.000 | 1.139 | 0.173 | 1.000 | 1.153 | 0.214 | 1.000 | 1.137 | 0.233 |
| 17_OMANU | 1.000 | 1.013 | 0.332 | 1.000 | 0.988 | 0.225 | 1.000 | 1.001 | 0.312 | 1.000 | 0.874 | 0.378 |
| 18_UTIL | 1.000 | 1.052 | 0.286 | 1.000 | 1.011 | 0.265 | 1.000 | 0.885 | 0.282 | 1.000 | 0.655 | 0.445 |
| 19_CONST | 1.000 | 1.408 | 0.105 | 1.000 | 1.298 | 0.105 | 1.000 | 0.897 | 0.396 | 1.000 | 0.930 | 0.289 |
| 20_TRCOTR | 1.000 | 0.995 | 0.308 | 1.000 | 0.783 | 0.448 | 1.000 | 0.641 | 0.476 | 1.000 | 0.842 | 0.372 |
| 21_SERV | 1.000 | 0.597 | 0.593 | 1.000 | 0.665 | 0.535 | 1.000 | 0.769 | 0.411 | 1.000 | 0.904 | 0.315 |
| p_w | 1.000 | 0.946 | 0.000 | 1.000 | 0.950 | 0.000 | 1.000 | 0.747 | 0.000 | 1.000 | 0.865 | 0.000 |
| p_m | 1.000 | 1.103 | -0.198 | 1.000 | 1.094 | -0.231 | 1.000 | 0.737 | 0.259 | 1.000 | 1.022 | -0.109 |
| $r$ | 0.484 | 0.511 | 0.000 | 0.441 | 0.479 | 0.000 | 0.568 | 0.672 | 0.000 | 0.459 | 0.511 | 0.000 |

References: Obs.: observed in actual data, Comp.: computed. Shaded cell indicates ( $\mathrm{M}-\mathrm{X}$ )/M
01_AGRIC to 21_SERV industries, p_w: price of a monetary unit of wage labour, $p$ _ $m$ : price of a monetary unit of imports
$r$ : mark-up on circulating capital and labour costs.

## Model-implied changes in relative prices



## Model-implied changes in income categories

(a) Import-substitution
$(1953)$
$(M-X) / M=-0.198$
(b) Structuralism
(1973)
$(M-X) / M=-0.231$
(c) Convertibility
(1997)
$(M-X) / M=-0.259$
(d) Post-Convert.
(2011)
$(M-X) / M=-0.109$


