## The general theory of labour value

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Accompanying paper:
ianwrightsite.files.wordpress.com/2017/04/general-theory-labour-value2.pdf

## Contents of paper

- Part 1: Linear production model
- Multiple measures of "labour value’
- "Labour embodied" equals "labour commanded" even with "profits on stock"


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- Part 1: Linear production model
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- "Labour embodied" equals "labour commanded" even with "profits on stock"
- Part 2: Nonlinear dynamic model
- Minimal model of the dynamics of classical competition
- A general law of value


## Plan of talk

- Part 1: Linear production model
- Multiple measures of "labour value"
- "Labour embodied" equals "labour commanded" even with "profits on stock"
- Part 2: Nonlinear dynamic model
- Minimal model of the dynamics of classical competition
- A general law of value


## Part 1: Linear production model

## A steady-state multi-sector economy



## Flows of goods



## Supply of labour



## Consumption of real wage



## Flows of payments



## Steady-state equilibrium



## Vertical integration

- How much coexisting labour is supplied to produce a commodity?


## Vertical integration iteration 1

0.2


## Vertical integration iteration 1



## Vertical integration iteration 1



## Vertical integration iteration 1



## Vertical integration iteration 2

0.2


## Vertical integration iteration 2



## Vertical integration iteration 2



## Vertical integration iteration 2



## We do not vertically integrate the real wage



## Labour costs are a terminus



## Vertical integration iteration 3



## Vertical integration iteration $n \rightarrow \infty$



## Classical labour values

$$
\mathbf{v}=\mathbf{I}\left(\mathbf{I}+\mathbf{A}+\mathbf{A}^{2}+\mathbf{A}^{3}+\ldots\right)
$$

vertical integration

## Classical labour values

$$
\begin{aligned}
\mathbf{v} & =\mathbf{I}\left(\mathbf{I}+\mathbf{A}+\mathbf{A}^{2}+\mathbf{A}^{3}+\ldots\right) \\
& =\mathbf{I}(\mathbf{I}-\mathbf{A})^{-1}
\end{aligned}
$$

vertical integration
vertically integrated subsystem

## Classical labour values

$$
\begin{aligned}
\mathbf{v} & =\mathbf{I}\left(\mathbf{I}+\mathbf{A}+\mathbf{A}^{2}+\mathbf{A}^{3}+\ldots\right) & & \text { vertical integration } \\
& =\mathbf{I}(\mathbf{I}-\mathbf{A})^{-1} & & \text { vertically integrated subsystem } \\
& =\mathbf{I}+\mathbf{v A} & & \text { direct plus indirect labour }
\end{aligned}
$$

Marx: new labour added plus transfer of labour 'embodied' in means of production

## Vertical integration

- How much coexisting labour is supplied to produce a commodity?


## Vertical integration

- How much coexisting labour is supplied to produce a commodity?
- Answer: classical labour values

$$
v=v A+I
$$

## Vertical integration

- How much coexisting labour is supplied to produce a commodity?
- Answer: classical labour values
$\mathrm{v}=\mathrm{vA}+\mathrm{l}$
- But did we really count all the coexisting labour?


## A steady-state multi-sector economy



## A steady-state multi-sector economy

capitalists


## A steady-state multi-sector economy



## Flow of profit income



## A steady-state multi-sector economy



## Vertical integration iteration 1

capitalists


## Vertical integration iteration 1

capitalists


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capitalists


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## Vertical integration iteration 3

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## Vertical integration iteration $n \rightarrow \infty$



## Super-integrated labour values

$$
\underline{\mathbf{v}}=\mathbf{I}\left(\mathbf{I}+(\mathbf{A}+\mathbf{C})+(\mathbf{A}+\mathbf{C})^{2}+(\mathbf{A}+\mathbf{C})^{3}+\ldots\right) \quad \text { vertical integration }
$$

## Super-integrated labour values

$$
\begin{aligned}
\underline{\mathbf{v}} & =\mathbf{I}\left(\mathbf{I}+(\mathbf{A}+\mathbf{C})+(\mathbf{A}+\mathbf{C})^{2}+(\mathbf{A}+\mathbf{C})^{3}+\ldots\right) & & \text { vertical integration } \\
& =\mathbf{I}(\mathbf{I}-(\mathbf{A}+\mathbf{C}))^{-1} & & \text { vertically super-integrated subsystem }
\end{aligned}
$$

## Super-integrated labour values

$$
\begin{aligned}
\underline{\mathbf{v}} & =\mathbf{I}\left(\mathbf{I}+(\mathbf{A}+\mathbf{C})+(\mathbf{A}+\mathbf{C})^{2}+(\mathbf{A}+\mathbf{C})^{3}+\ldots\right) & & \text { vertical integration } \\
& =\mathbf{I}(\mathbf{I}-(\mathbf{A}+\mathbf{C}))^{-1} & & \text { vertically super-integrated subsystem } \\
& =\mathbf{I}+\underline{\mathbf{v}}+\underline{\mathbf{v} \mathbf{C}} & & \begin{array}{l}
\text { direct plus indirect plus } \\
\text { super-indirect labour }
\end{array}
\end{aligned}
$$

## Vertical integration

- How much coexisting labour is supplied to produce a commodity?
- Answer: classical labour values
$\mathrm{v}=\mathrm{vA}+\mathrm{l}$
- But did we really count all the coexisting labour? No.


## Vertical integration

- How much coexisting labour is supplied to produce a commodity?
- Answer: classical labour values

$$
v=v A+I
$$

- But did we really count all the coexisting labour? No.
- Correct answer: super-integrated labour values

$$
\underline{v}=\underline{v} \mathbf{A}+\underline{v} \mathbf{C}+\mathbf{I}
$$

## Super-integrated labour values

- The capitalist consumption matrix, $\mathbf{C}$, is a function of the technique, $\mathbf{A}$ and $\mathbf{I}$, and real income, w (real wage) and $\mathbf{c}$ (capitalist consumption).


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- The total working day, Iq, equals the super-integrated labour value of the real wage, $\mathbf{l q}=\underline{\mathbf{v}} \mathbf{w}$.
- Hence, $\mathbf{l q}=\mathbf{v}(\mathbf{w}+\mathbf{c})=\underline{\mathbf{v}} \mathbf{w}$


## Equilibrium prices and labour costs

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- Theorem:

The prices of a steady-state economy are proportional to
super-integrated labour values, $\mathbf{p}=\underline{\mathbf{v}} \mathrm{w}$, where w is wage rate.

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- Theorem:

The prices of a steady-state economy are proportional to super-integrated labour values, $\mathbf{p}=\underline{\mathbf{v}} \mathrm{w}$, where w is wage rate.

- "Labour embodied" equals "labour commanded" even with "profits on stock"
- A general theory:
- Technical measures of labour value
- Social measures of labour value


## Further details

- "The general theory of labour value". ianwrightsite.files.wordpress.com/2017/04/general-theory-labour-value2.pdf
- "A category mistake in the classical labour theory of value". Erasmus Journal for Philosophy and Economics 7 (1), 27-55. 2014.
- "Marx's transformation problem and Pasinetti's vertically-integrated subsystems". Forthcoming in the Cambridge Journal of Economics.
- "The Law of Value: A contribution to the classical approach to economic analysis". PhD Thesis, Open University. 2015.


## Additional material

